

MATHEMATICS 322

ASSIGNMENT 5

Due: October 7, 2015

01• Let $I = [0, 1]$ and let $J = [0, \infty)$. Let f be a complex valued function defined on I and let γ be a complex valued function defined on $J \times I$ which meets the conditions:

$$(H) \quad \begin{aligned} \gamma_t(t, x) &= \gamma_{xx}(t, x) \\ \gamma(0, x) &= f(x) \end{aligned}$$

where $0 \leq t$ and $0 \leq x \leq 1$. The foregoing assembly (H) is a simple form of the Heat Equation. One may interpret $\gamma(t, x)$ as the *temperature* at time t at the position x in the *rod* I . Given f , find various solutions γ by the method of Separation of Variables:

$$\gamma(t, x) = \alpha(t)\beta(x)$$

Of course, you may form linear combinations of the solutions you find. In particular, find solutions subject to the following boundary conditions:

$$(1) \quad \gamma(t, 0) = 0 \text{ and } \gamma(t, 1) = 0$$

Do the same for the cases:

$$(2) \quad \gamma_x(t, 0) = 0 \text{ and } \gamma(t, 1) = 0$$

$$(3) \quad \gamma(t, 0) = 0 \text{ and } \gamma_x(t, 1) = 0$$

and, finally, for the case:

$$(4) \quad \gamma_x(t, 0) = 0 \text{ and } \gamma_x(t, 1) = 0$$